Motion Control of the CyberCarpet Platform

Alessandro De Luca, Fellow, IEEE, Raffaella Mattone, Paolo Robuffo Giordano, Member, IEEE, Heinz Ulbrich, Martin Schwaiger, Michael Van den Bergh, Member, IEEE, Esther Koller-Meier, and Luc Van Gool

Abstract—The CyberCarpet is an actuall platform that allows unconstrained locomotion of a walking user for Virtual Reality exploration. The platform consists of a linear treadmill covered by a ball-array carpet and mounted on a turntable, and is equipped with two actuating devices for linear and angular motion. The main control objective is to keep the walker close to the platform center in the most natural way, counteracting his/her voluntary motion while satisfying perceptual constraints. The motion control problem for this platform is not trivial since the system kinematics is subject to a nonholonomic constraint. In the first part of the paper we describe the kinematic control design devised within the CyberWalk project, where the linear and angular platform velocities are used as input commands and feedback is based only on walker’s position measurements obtained by an external visual tracking system. In particular, we present a globally stabilizing control scheme that combines a feedback and a feedforward action, based on a disturbance observer of the walker’s intentional velocity. We also discuss possible extensions to acceleration-level control and the related assessment of dynamic issues affecting a walker during his/her motion. The second part of the paper is devoted to the actual implementation of the overall system. As a proof of concept of a full-scale platform, the mechanical design and realization of a small-scale prototype of the CyberCarpet is presented, as well as the visual localization method used to obtain the human walker’s position on the platform by an overhead camera. To validate the proposed motion control design, experimental results are reported and discussed for a series of motion tasks performed using a small tracked vehicle representative of a moving user.

Index Terms—Disturbance observer, input-output feedback linearization, locomotion platform, motion control, nonholonomic systems, virtual reality (VR), visual tracking.

I. INTRODUCTION

EXPLORATION of virtual reality (VR) worlds by allowing omni-directional unconstrained locomotion possibilities for a walking user is an active area of research. The final goal is having the user fully immersed in a VR scene viewed by, e.g., a head mounted display (HMD), free to walk in any direction with natural speed, while remaining within the limited physical area of a platform and without the need of wearing any constraining equipment (e.g., for tracking the walker position or for characterizing the gait). To support locomotion in this way, the platform should counteract the intentional motion of the walker in order to keep him/her in place. In doing so, the associated perceptual effects on the walker should be taken into account, in the form of input command constraints, so as to avoid disruptive effects on the user’s immersiveness. These have been the main objectives of the European research project CyberWalk [1].

Different locomotion interfaces exist that allow walking in virtual environments (see, e.g., the surveys in [2]–[4]). In many of them, locomotion is restricted to a 1-D motion on a linear treadmill, like in the Treadport platform [5] with possible slope inclusion [6]. The user is constrained by a harness to apply stabilizing forces and other virtual effects [7]. To allow for small/slow direction changes, the treadmill can be mounted on a turning table [8]. A different approach is taken in the CirculaFloor [9], where active moving tiles follow the feet motion. Again, the walker should avoid sharp turns and high speed. For unconstrained 2-D walking, the Omnidirectional Treadmill has been proposed in [10] using two perpendicular belts and a large number of rollers, while a torus-shaped belt arrangement is implemented in the Torus Treadmill [11]. Both systems allow limited speed, mostly due to poor control design. Furthermore, the mechanical implementation is critical due to the large mass of the moving parts (associated noise). This kind of problems is not present in passive devices like the Cybersphere [12] where, however, the naturalness of walking is limited by the inner curvature of the spherical floor. An alternative principle is used in [13], where a conveyor belt and a turntable transmit motion to a walker through a ball-array board, realizing thus a 2-D planar treadmill. In [14], the ball-array lays on a concave surface without actuation, but instrumented with sensors to detect feet contact.

Within the CyberWalk project, two different motion concepts have been considered for unconstrained 2-D walking on a plane: the omnidirectional belt-array CyberWalk platform [15]–[17] (similar to [10] and [11]), and the ball-array CyberCarpet [18]–[20] (similar to [13]). In both cases, as project requirements, we wished to eliminate the use of any physical constraints on the feet, body, or legs of the user, as well as to...
avoid the need of a priori or identified models of the human gait/walk. The two platform concepts have been analyzed and refined in terms of user mobility, mechanical feasibility, and perceptual effects.

In this paper, we focus on the CyberCarpet and its motion control problem. This locomotion platform uses a conveyor belt and a turntable to transmit translational and angular motion to the walker through a ball-array board. Rotating balls are formed into an array and are in contact with the belt so that a user on the board moves in the opposite direction of the underlying point on the belt, see Fig. 1(a). The walker will be allowed to move in a natural way and indefinitely in any planar direction. In fact, the platform controller will counteract her/his motion by pulling the walker toward the center of the platform, while taking into account physiologically acceptable velocity/acceleration bounds. The body pose on the carpet is acquired through a markerless visual tracking system using an overhead camera.

As a proof of concept of the CyberCarpet principle, a small-scale prototype of about 0.8 m of diameter has been designed and built, see Fig. 1(b). The overall system architecture is shown in Fig. 2. While the limited platform dimension is indeed not appropriate for the actual VR exploration by a human user, the whole system has been conceived keeping in mind the requirements and challenges of a full-size realization. In fact, the current mechanical structure can already support the weight of a human user (about 100 kg). Further, our proposed control design allows a straightforward scaling of control gains to the platform size and locomotion speed of the walker, and extensions to acceleration level control make it possible to fully take into account dynamic issues affecting the walker during her/his motion. Finally, the visual tracking algorithm has been tested on human walkers and proved to be robust w.r.t. her/his posture changes (see Fig. 16). To show the effectiveness of the platform control design, we report experimental results in which a top-view human picture has been mounted on a mobile robot and used as a mock-up to emulate the motion behavior of a real user (see Fig. 17).

From the control point of view, one challenging issue is due to the kinematic model of the system, which is highly nonlinear as opposed to the case of other 1-D and 2-D omnidirectional platforms, and it includes a nonholonomic constraint on the system instantaneous velocities. While the platform cannot provide full local mobility to the user, we will design a control law that achieves smooth and global regulation of the walker position from any initial configuration. Previous works on locomotion interfaces have paid little attention to control issues and algorithms, relying mostly on very simple proportional-integral-derivative (PID) laws or heuristic schemes. With the notable exception of [21] for a 1-D treadmill, no stability analysis has been considered previously. Moreover, performance in 2-D has been predicted only by restricting motion to low and piece-wise constant walker velocity with few directional changes (see, e.g., the paper by [13] on a similar ball-array locomotion device). In contrast, a complete motion control design is presented here for the 2-D CyberCarpet platform, together with a detailed analysis of the closed-loop performance. A number of experimental results are included to validate our approach.

This paper is organized as follows. In the first part, we present the control approach devised within the CyberWalk project.1 The kinematic model of the CyberCarpet platform is given in Section II, and its duality with the control problem for nonholonomic wheeled robots is pointed out. In Section III, we propose a velocity control scheme based on input-output decoupling and linearization (see Section III-A), which shows an acceptable overall performance but is still affected by some singularities that prevent global stabilization results. The velocity control scheme is then suitably modified in order to avoid such singularities (see Section III-B), and an additional feedforward action is used, based on a disturbance observer of the (unavailable) intentional velocity of the walker (see Section III-C). Performance of this controller is much more satisfactory and is first validated by numerical simulations (see Section III-D). Finally, a convenient way to extend the design by considering accelerations as control inputs is discussed in Section IV. This allows to take explicitly into account acceleration bounds imposed by the actuation system and the perception of the human walker. A simplified analysis of the dynamic effects that a user would experience is also included (see Section IV-A).

The second part of the paper is devoted to the physical implementation and test of a small-scale but complete prototype of the CyberCarpet. Section V illustrates the mechanical design and the hardware realization. Section VI describes the visual tracking algorithm for the localization of the absolute walker position (and orientation) on the platform, based on

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1Preliminary versions of this part have been presented in the conference papers [18]–[20].
particle filters. Experimental results are reported in Section VII, showing the performance of the implemented velocity-level control laws within the integrated system. Videos of all experiments are included in the accompanying material to this paper, as well as available at http://www.dis.uniroma1.it/labrob/research/CW.html together with further illustrating movies. Conclusions and future work are discussed in the final section, including also a comparison with the companion omnidirectional belt-array CyberWalk platform.

II. KINEMATIC MODEL

Thanks to the ball-array surface of the CyberCarpet, any actuated motion of the underlying belt will result in a reverse motion imposed on the walker on the platform, i.e., a forward motion command will move the user backwards and, due to the multiple contact between walker’s feet and the ball-array carpet, a clockwise rotation will turn the user counterclockwise—see Fig. 1(a).

With this in mind, it is possible to derive a kinematic model of the CyberCarpet. With reference to Fig. 3, let \( \{X_0, Y_0\} \) be the absolute inertial frame (attached to the fixed overlooking camera) and \( \{X_t, Y_t\} \) is the frame attached to the (rotating) treadmill, with the \( X_t \)-axis in the direction of the belt, rotated by an angle \( \theta \) w.r.t. \( X_0 \). Both frames have the origin at the center of the CyberCarpet. The walker absolute position and orientation are, respectively, \( \{x, y\} \) and \( \theta_w \), with the distance from the center \( R = \sqrt{x^2 + y^2} \) and the angle \( \alpha = \text{ATAN2}(y, x) - \theta \) locating the walker in polar coordinates w.r.t. the rotating frame \( \{X_t, Y_t\} \).

When the walker is standing still, we have

\[
\begin{align*}
\dot{x} &= -v \cos \theta + y \omega \\
\dot{y} &= -v \sin \theta - x \omega \\
\dot{\theta} &= \omega \\
\dot{\theta}_w &= -\omega.
\end{align*}
\]

(1)

In (1), \( v \) and \( \omega \) are the commanded linear and angular velocity of the CyberCarpet. These are applied on the bottom of the ball-array, which explains the minus signs appearing in the first, second, and fourth equation of the model.

For \( R \neq 0 \), the two Cartesian coordinates \( \{x, y\} \) may also be replaced by the polar coordinates \( \{R, \alpha\} \) (see also [22]), obtaining

\[
\dot{R} = -v \cos \alpha, \quad \dot{\alpha} = v \sin \alpha - \omega - 2 \omega.
\]

(2)

A simple analysis of the kinematic (1) shows that a holonomic constraint exists

\[
\theta + \theta_w = \theta(0) + \theta_w(0) = \text{constant}
\]

(3)

i.e., the change of orientation of the platform under control will be equal to the opposite of the change of orientation of the walker (when standing still). Therefore, only one of these two variables can be independently controlled. However, this is not a limitation for the considered motion control task. When a platform user walks through a virtual world (e.g., wearing an HMD), the relevant orientation for a correct VR visualization is only the one intentionally assumed by the walker head, which is fully unrelated from the platform orientation \( \theta \) and partially independent from the orientation \( \theta_w \) of the user body.

On the other hand, in the 3-D configuration space of interest, parametrized by \( \{x, y, \theta\} \), the system is subject to the differential constraint

\[
\begin{bmatrix}
\sin \theta & \cos \theta & -x \cos \theta + y \sin \theta
\end{bmatrix}
\begin{bmatrix}
\dot{x} \\
\dot{y} \\
\dot{\theta}
\end{bmatrix} = 0.
\]

(4)

This constraint implies that the platform cannot move the position \( \{x, y\} \) of the walker along the direction of the axis \( Y_t \). As a consequence, the platform will not be able to cancel instantaneously a walker linear velocity in that direction. Nonetheless, (4) is nonholonomic (i.e., it cannot be integrated to a positional constraint) and thus the nonlinear system is fully controllable to any desired configuration \( \{x, y, \theta\} \) [23]. Therefore, re-centering of a standing user to the platform origin \( 0, 0, 0 \) can be in principle achieved by suitable platform maneuvers obtained by the control commands \( v \) and \( \omega \). It is interesting to note that, in view of (4), the motion control problem for the CyberCarpet is similar to that of nonholonomic wheeled mobile robots. The analogy of the two problems can be intuitively recognized also by flipping things upside down: the standing user plays the role of the fixed ground, while the nonholonomic platform will act as the controlled wheeled mobile robot.

However, the above duality is lost when the walker starts to move. In fact, when the walker is in motion, the model (1) becomes

\[
\begin{align*}
\dot{x} &= -v \cos \theta + y \omega + V_{w,x} \\
\dot{y} &= -v \sin \theta - x \omega + V_{w,y} \\
\dot{\theta} &= \omega \\
\dot{\theta}_w &= -\omega + \Omega_w.
\end{align*}
\]

(5)

where \( V_w = \{V_{w,x}, V_{w,y}\} \) and \( \Omega_w \) are, respectively, the absolute linear and angular walker intentional velocities (see Fig. 3). These are clearly unknown in advance and not directly measurable. In the following, the walker intentional velocities will be considered as disturbances in the control design. In particular, we will not be interested in \( \Omega_w \) since this exogenous signal
will not affect the walker position on the platform. Instead, the walker displacement due to the linear velocity vector $V_w$ needs to be rejected by the control system.

III. CONTROL DESIGN

A number of feedback control laws developed for nonholonomic wheeled mobile robots can be adapted to address the regulation problem for the CyberCarpet, so as to bring the position (and, if needed, the orientation too) of a standing user to zero. These techniques include Lyapunov design in polar coordinates [22], time-varying nonlinear control [24], control based on the chained-form transformation or on system flatness [25], or recursive control with backstepping [26]. Although successful, these techniques lead to somewhat oscillatory and/or slow transients that are not compliant with user perceptual constraints. Moreover, the extension of such control laws to handle the persistent disturbance due to the motion of the walker has not been considered yet.

The nature of our motivating application (locomotion of a user in a VR environment using an HMD) specifies the control task as regulation of only the position $(x, y)$ of the walker. In this respect, the walker’s position can be asymptotically stabilized to the platform origin using a simpler control design based on input-output feedback linearization.

A. Input-Output Decoupling and Linearizing Control

Consider first the case of no disturbances, i.e., $V_w = 0$ and $\Omega_w = 0$ (walker standing still in the virtual environment) and define the controlled output as $(x, \theta)$. From (1), it is

$$\begin{bmatrix} \dot{x} \\ \dot{y} \end{bmatrix} = \begin{bmatrix} -\cos \theta & y \\ -\sin \theta & -x \end{bmatrix} \begin{bmatrix} v \\ \omega \end{bmatrix} = A(x, y, \theta) \begin{bmatrix} v \\ \omega \end{bmatrix}. \quad (6)$$

When $\det A = x \cos \theta + y \sin \theta \neq 0$, we can set

$$\begin{bmatrix} \tau \\ \omega \end{bmatrix} = A^{-1}(x, y, \theta) \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} \quad (7)$$

where $v_1$ and $v_2$ are auxiliary velocity inputs to be defined. The resulting input-output behavior is given by simple integrators

$$\dot{x} = v_1, \quad \dot{y} = v_2$$

i.e., it has been decoupled and linearized by the feedback law (7). The control design can be completed by the proportional laws

$$v_1 = -k_1 x, \quad v_2 = -k_2 y \quad (8)$$

with positive gains $k_i, i = 1, 2$, thus exponentially stabilizing the walker’s position to the origin.

An interesting property of the designed controller is the following. With the walker standing at an initial position $(x_0, y_0)$, the controlled time evolution of his/her position will be $x(t) = e^{-k_1 t} x_0$ and $y(t) = e^{-k_2 t} y_0$. Choosing $k_1 = k_2$ leads to

$$\frac{y(t)}{x(t)} = \frac{\dot{y}(t)}{\dot{x}(t)} = \frac{y_0}{x_0}$$

so that the user will be pulled toward the origin along the connecting straight line.

For the purpose of analysis, an equivalent expression for the control law $v$ and $\omega$ can be found by selecting (from now on) equal gains $k_1 = k_2 = k > 0$ and replacing (8) into (7). This yields

$$v = \frac{k(x^2 + y^2)}{x \cos \theta + y \sin \theta} = \frac{k R^2}{R \cos \alpha} = \frac{k R}{\cos \alpha} \quad (9)$$

and

$$\omega = \frac{k(y \cos \theta - x \sin \theta)}{x \cos \theta + y \sin \theta} = \frac{k R \sin \alpha}{R \cos \alpha} = k \tan \alpha. \quad (10)$$

The control law (9), (10) has the singularity $R \cos \alpha = x \cos \theta + y \sin \theta = 0$ (where the determinant of the decoupling matrix is zero), i.e., when the walker is on the $Y_r$-axis (in particular, at the origin). Note that the singularity at the origin is hidden, in polar coordinates, by the fact that the angle $\alpha$ is not defined there. In the following, we will introduce modifications that overcome these control singularities, while preserving the convenient characteristics of the decoupling law (9), (10). We still consider for the time being the case of no disturbances, $V_w = 0$ and $\Omega_w = 0$ (walker standing still in the virtual environment), dealing later with the case of walker in motion (see Section III-C).

B. Handling the Singularities at $\cos \alpha = 0, R = 0$

When $R \neq 0$, the control singularity at $\alpha = \pm(\pi/2)$ can be eliminated by taking

$$v = kR \text{sgn}(\cos \alpha) \quad (11)$$

and

$$\omega = k \sin \alpha \text{sgn}(\cos \alpha) \quad (12)$$

with $\text{sgn}(\arg) = 1$ for $\arg \geq 0$ and $\text{sgn}(\arg) = -1$ otherwise. The control law (11), (12) is formally obtained by multiplying (9), (10) by $\cos \alpha$. The resulting input-output dynamics is now

$$\dot{x} = -k \cos \alpha x, \quad \dot{y} = -k \cos \alpha y \quad (13)$$

which is no longer linear nor decoupled, since the angle $\alpha$ depends on both $x$ and $y$. However, from (13) it follows:

$$\frac{y(t)}{x(t)} = \frac{\dot{y}(t)}{\dot{x}(t)} = \frac{y_0}{x_0} \quad (14)$$

as before. Therefore, a standing user will still be driven along the straight line connecting its initial position to the origin ($\dot{\theta} = \dot{\alpha} = 0$ and $\beta(t) = \beta_0 := \beta_0$ is constant).

In order to show that the control law (11), (12) is also asymptotically stabilizing the walker position $(x, y)$ to the origin, consider the positive definite Lyapunov function

$$V(x, y, \theta) = \frac{1}{2} \left( x^2 + y^2 + \sin^2(\beta_0 - \theta) \right) \quad (15)$$

with $V = 0$ if and only if $(x, y, \theta)$ belongs to the set $S = \{(0, 0, \theta) : \sin(\beta_0 - \theta) = 0\}$. Using (2), the time derivative
of \( V \) along the trajectories of the closed-loop system (1), (11), (12) is given by
\[
\dot{V} = R \dot{R} + \sin \alpha \cos \alpha \dot{\alpha} = -k \cos \alpha (R^2 + \sin^2 \alpha)
\]
\[
= -2k \cos \alpha V \leq 0
\]
(16)
so that \( \dot{V} = 0 \) for \((x, y; \theta) \in \mathcal{S} \), as well as for \( \cos \alpha = 0 \). However, the latter does not correspond to closed-loop system equilibria since then \( \omega = +k \) and thus \( \theta \) cannot be constant. Therefore, \( \mathcal{S} \) is the (largest) invariant set where \( V = 0 \), and \((x, y)\) will converge to the origin by virtue of LaSalle theorem.

At \( R = 0 \), the control law (11), (12) is clearly discontinuous at the origin \( x = y = 0 \), due to the discontinuity of the angle \( \alpha \) which is not defined there. This causes a chattering of the control input \( \omega \) when the walker is in a small region around the platform center. In order to avoid this problem, we proposed in [19] the introduction of a dead zone around the origin. However, when the walker is in motion, the chattering of the input commands may appear again at the border of the dead zone.

A more effective solution is obtained by replacing the feedback control law (11), (12) with
\[
v = kR^2 \text{sgn}(\cos \alpha) = k(x^2 + y^2) \text{sgn}(x \cos \theta + y \sin \theta)
\]
(17)
and
\[
\omega = kR \sin \alpha \text{sgn}(\cos \alpha)
\]
\[
= k(y \cos \theta - x \sin \theta) \text{sgn}(x \cos \theta + y \sin \theta)
\]
(18)
which are formally obtained multiplying (11), (12) by the radial distance \( R \). The control law (17), (18) is now well defined and continuous at any system configuration. In fact, the angular velocity command \( \omega \) converges to zero as \((x, y)\) approaches the origin, so that no chattering occurs in this case. Under the feedback law (17), (18) and in the absence of walker motion, the behavior of the controlled outputs becomes
\[
\dot{x} = -kR \cos \alpha |x|, \quad \dot{y} = -kR \cos \alpha |y|
\]
(19)
which can be proved to be asymptotically stable at the origin by the same Lyapunov arguments used for law (11), (12). Furthermore, (14) still holds in this case, i.e., the user is pulled toward the origin along the connecting straight line. However, the convergence rate of the \( x \) and \( y \) variables drops quadratically to zero as the walker approaches the origin.

Remark 1: A Lyapunov-based proof of stability for the control law (17), (18) holds also in the case of a varying gain \( k \), provided that \( k > 0 \). This property can be used to decrease excessively large commands \( v \) and/or \( \omega \) in order to comply with human perceptual constraints. In particular, assume that the control inputs should remain always bounded as
\[
|v| \leq v_{\text{max}}, \quad |\omega| \leq \omega_{\text{max}}
\]
(20)
and choose a convenient \( k > 0 \) to be used in (17), (18) in the unsaturated case. Then, the following scaling law for \( k \)
\[
k = \frac{k}{\max \left\{ 1, \frac{|w|}{v_{\text{max}}}, \frac{|w|}{\omega_{\text{max}}} \right\}} > 0
\]
(21)
will comply with the bounds in (20).

C. Dealing With Walker’s Velocity

When the walker is in motion, \( V_w \) and \( \Omega_w \) are in general both different from zero and the system kinematics is described by (5). A persistent walker locomotion will typically prevent the convergence of her/his position to the platform center when using the control law (17), (18). In particular, when the user walks indefinitely with constant velocity \( \dot{V} \) along a straight line in the virtual environment, a steady-state position will be reached under the control law (9), (10) at a distance \( \tilde{R} = \dot{V}/k \) from the origin. Using standard results from linear control theory, we proposed in [18] to add an integral control action so as to completely eliminate the steady-state error in the case of a constant walker velocity. However, use of an integral control action suffers from the typical position overshooting and leads to a poor dynamic performance for more general motion profiles of the walker.

Therefore, we follow a different approach to deal with the walker’s intentional motion, based on an estimate \( \dot{V}_w \) of the walker linear velocity vector \( V_w \). This allows to add suitable feedforward terms in the control law as
\[
v = v_{\text{fb}} + v_{\text{ff}} = v_{\text{fb}} + |\cos \theta| \sin \theta \dot{V}_w
\]
\[
\omega = \omega_{\text{fb}} + \omega_{\text{ff}} = \omega_{\text{fb}} + \text{sat} \left( \frac{1}{R} - |\sin \theta| \cos \theta \right) \dot{V}_w
\]
(22)
where the relabeled \( v_{\text{fb}} \) and \( \omega_{\text{fb}} \) are the feedback contributions given by (17), (18), and \( \text{sat}(\cdot) \) is the standard saturation function, with lower/upper saturation limits \( \pm \omega_{\text{ff, max}} \). It is readily verified that, for \( V_{w} = V_{w, s} \), the feedforward term \( v_{\text{ff}} \) in (22) compensates for the component of the walker velocity along the treadmill direction of the CyberCarpet, while \( \omega_{\text{ff}} \) (in the absence of saturation) cancels the component of \( V_{w} \) in the orthogonal direction.

Remark 2: When the control scaling strategy (21) is considered (see Remark 1), it should be applied only to the feedforward part in (22), i.e., with \( v = v_{\text{ff}} \) and \( \omega = \omega_{\text{ff}} \). In fact, the feedforward terms \( v_{\text{ff}} \) and \( \omega_{\text{ff}} \) in (22) result in a partial or perfect cancellation of the walker intentional velocity. In the absence of a position error, this control action is not “felt” by the user since he/she would be walking in place in the absolute frame. As a result, these feedforward terms should not be subject to perceptual constraints during walking, which instead limit the feedback part of the control law (22).
In order to get an estimate $\tilde{V}_w = (\tilde{V}_{w,x}, \tilde{V}_{w,y})$, consider the two scalar dynamical systems

$$\dot{\xi}_x = -v \cos \theta + y \omega + k_u (x - \xi_x)$$
$$\dot{\xi}_{x} = k_u (x - \xi_x)$$  (23)

and

$$\dot{\xi}_y = -v \sin \theta - x \omega + k_u (y - \xi_y)$$
$$\dot{\xi}_{y} = k_u (y - \xi_y)$$  (24)

where $k_u > 0$ and $v$ and $\omega$ are given by (22). Equations (23) and (24) have the structure of disturbance observers, respectively, with state $\xi_x$ and $\xi_y$. From these and (5), it follows:

$$\ddot{V}_{w,x} = k_u (V_{w,x} - \tilde{V}_{w,x}),$$
$$\ddot{V}_{w,y} = k_u (V_{w,y} - \tilde{V}_{w,y})$$

i.e., the estimates $\tilde{V}_{w,x}, \tilde{V}_{w,y}$ are low-pass filtered versions of the Cartesian components of $V_w$. In particular, for $k_u$ large enough, they accurately reproduce the two components $V_{w,x}$ and $V_{w,y}$ of the intentional walker velocity, expressed in absolute coordinates.

Note that, even after the feedforward compensation (22), the system is still affected by a residual disturbance

$$V_w - \tilde{V}_w = \frac{N}{s + k_u} V_w.$$  

Therefore, while walker’s constant velocities are fully compensated at steady state for any positive $k_u$, for walker’s ramp-wise velocities (constant accelerations) the associated steady-state error can only be made arbitrarily small by increasing $k_u$—an astatic velocity disturbance behavior is recovered by the proposed feedback/feedforward controller.

D. Simulation Results

We present here two selected results obtained with the singularity-free velocity control law discussed in Sections III-B and III-C. In both case studies, the walker starts at rest from the initial absolute position $(0, 1)$ m—one that would immediately lead to singularity for the control law (9), (10) of Section III-A.

Figs. 4–6 refer to the walker moving indefinitely along a straight line directed along the $y_0$-axis in the virtual space, and with a constant speed of 1 m/s (at time $t = 0$, it is $X_t(0) = X_0$). The platform is controlled by the combined feedback/feedforward scheme (22), wherein the feedback law (17), (18) and the disturbance observers (23), (24) are used. The associated control parameters are: $k = 1$ (i.e., $k$ without the scaling), $k_u = 10$, and $\Omega_{ff, \text{max}} = 2 \text{ rad/s}$ for the saturation term in (22). Moreover, in order to show the effects of a limitation of the velocity commands imposed by perceptual constraints, we have set a maximum value of 0.5 m/s and 0.1 rad/s, respectively, for $v_{fb}$ and $\Omega_{fb}$ in the feedback part (17), (18) of the control law (22). In Fig. 4, the actual motion of the walker in the absolute space is shown, with the absolute orientation of the walker being displayed by a segment. At the start, we have $\theta(t) = 0$ and $\theta_u(0) = \pi/2$. The overall behavior of the linear and angular velocity commands is shown in Fig. 5, while Fig. 6 shows only the feedback part of these velocity inputs. When the bounds set for the feedback part are exceeded, in particular at the beginning of the control interval until $t \approx 10$ s, the gain $k$ is lowered according to (21).

As an example of a more complex motion, we report the results for the virtual square path with 3 m sides shown in Fig. 7. The walker starts at rest and moves along each edge with a trapezoidal velocity profile, having symmetric acceleration/deceleration phases with $2.4 \text{ m/s}^2$ for 0.5 s each and a cruise velocity of 1.2 m/s kept for 2 s. At each reached corner, the walker stops and turns counterclockwise with an angular speed of $\pi/2 \text{ rad/s}$. Thus, the total trajectory of the walker lasts 16 s. Without motion control of the platform, the walker would exit from the platform circular boundary set at a radius of 2.5 m.

The control parameters are chosen as before. In order to evaluate the performance attainable by the proposed control scheme, no perceptual constraints on the feedback commands are considered in this second case. The results are shown in Figs. 8 and 9. Thanks to the combined feedback and feedforward actions, the walker is rapidly brought close to the platform center and then kept there. The linear control input is again smooth and, after an
initial transient, does never exceed the walker’s voluntary speed. On the other hand, saturation on the angular feedforward term (with $\omega_{ff,\max} = 2$ rad/s as before) comes into action when the walker is close to the origin and takes a sharp turn (starting with the corner after Edge 2 of the path). Note that the platform lags behind during each turn performed on place by the walker, since a walker’s angular motion without linear displacement triggers no feedforward action.

IV. EXTENSION TO ACCELERATION-LEVEL CONTROL

In order to take into account limitations on linear and angular accelerations imposed by the actuators and/or by perceptual constraints, an acceleration-level control design is more suitable. To this end, the presented smooth velocity-level control law can be transformed to the acceleration level using the theory of cascaded systems, see, e.g., [27], or backstepping techniques, see, e.g., [28]. Moreover, the availability of platform accelerations allows the analytical computation of the apparent accelerations felt by a walking user. This possibility is especially relevant for the evaluation of dynamic effects on the walker in a full-scale version of the CyberCarpet platform.

To pursue an acceleration-level control design, a second-order version of the kinematic model (5) must be considered. This is obtained by simply extending the first-order kinematic models (1) and (5) with the equations

$$\dot{v} = a, \quad \dot{\omega} = \eta \tag{25}$$

where $a$ and $\eta$ are, respectively, the linear and angular acceleration commands of the platform. When a control law for the regulation objectives stated in Section III has to be designed on the extended (second-order) system (5)–(25), the availability of smooth stabilizing laws $v = v_q(x, y, \theta)$ and $\omega = \omega_q(x, y, \theta)$ for the first-order system (5) can be exploited. In the following, we present the design for cascaded systems.

The stability of a cascaded system in the form

$$\dot{\xi}_1 = f_1(t, \xi_1) + g_1(t, \xi_1, \xi_2) \xi_2, \quad \dot{\xi}_2 = f_2(t, \xi_2) \tag{26}$$

can be concluded, under mild conditions, from the stability of the two subsystems $\dot{\xi}_1 = f_1(t, \xi_1)$ and $\dot{\xi}_2 = f_2(t, \xi_2)$ (see
In order to use this result, we transform system (5)-(25) in the form (26) by defining  

\[ \zeta_1 = \begin{bmatrix} x \\ y \\ \theta \end{bmatrix}, \quad \xi = \begin{bmatrix} v \\ \omega \end{bmatrix}, \quad \xi_d = \begin{bmatrix} v_d \\ \omega_d \end{bmatrix} \]

\[ \zeta_2 = \xi - \xi_d, \quad u(t) = \begin{bmatrix} u(t) \\ \eta(t) \end{bmatrix}. \]

The system equations become

\[ \dot{\zeta}_1 = A(\zeta_1)\xi_d(t, \zeta_1) + A(\zeta_1)\zeta_2 \]  
\[ \dot{\zeta}_2 = u(t) - \frac{d\xi_d(t)}{dt} \]  

where \( A(\zeta_1) \) is defined in (6). Equations (27), (28) take the form (26) with \( f_1(t, \zeta_1) = A(\zeta_1)\xi_d(t, \zeta_1), \) \( g_i(\zeta_1) = A(\zeta_1), \) and \( f_2(t) = u(t) - \frac{d\xi_d(t)}{dt}. \)

From Section III, we know already that the “downstream” system (27) is asymptotically stable for \( \zeta_2 = 0, \) i.e., for \( \xi = \xi_d. \) In order to stabilize the overall cascaded system, it is then sufficient to stabilize the “upstream” system (28) to the origin, i.e., to bring \( \zeta_2 \) to zero. This can be easily obtained by choosing, for any positive definite matrix \( K \)

\[ u = \dot{\xi}_d - K\zeta_2 = \dot{\xi}_d - K(\xi - \xi_d). \]  

The control law (29) requires the differentiability of the first-order velocity control law \( \xi_d. \) Indeed, (17), (18) are not differentiable at configurations where the argument of the sgn function is zero. This problem, however, can be overcome by setting \( \xi_d = 0 \) in (29) at such configurations. Note also that an analytical expression of \( \xi_d \) can be computed from (17), (18) and the model (5), (25), where the walker velocity \( V_w \) is treated locally as a constant.

The above control design has been compared to a backstepping approach in [20], and their relative performance as well as those of acceleration versus velocity-level control have been evaluated by simulations on the CyberCarpet. The reader is referred to [20] for the numerical results. The general outcome is that a very similar behavior is obtained, with slightly longer regulation transients but smoother resulting velocities when acceleration control is applied.

**A. Dynamic Effects of Platform Motion on the Walker**

Due to the platform motion, the “virtual world” frame attached to the walker is in general non-inertial. In particular, even when the intentional velocity of the walker is constant, she/he will feel “apparent” accelerations (and thus forces) due to the rotation and/or non-uniform translation of the carpet. One major advantage of moving the control action to the acceleration level is that these accelerations can be reliably computed in closed form.

In particular, when walking at constant velocity \( \dot{V}_w \) in the non-inertial virtual world, the apparent acceleration felt by the user equals the opposite of her/his absolute acceleration. This is obtained by analytic differentiation of the first two equations in (1), using (25) and the acceleration control law (29). The apparent acceleration \( \ddot{a} \) felt by the user can be decomposed into three different components depending, respectively, on the linear and angular accelerations of the frame \( \{X_i, Y_i, Z_i\} \) (inertial acceleration), on the square of the angular velocity of this frame (centrifugal acceleration), and on the coupling between its angular velocity and the walker relative velocity (Coriolis acceleration). These components should be expressed in the frame \( \{X_w, Y_w, Z_w\} \) attached to the walker, see Fig. 3, in order to evaluate their effects on the user. The results of these computations are reported below, where \( \text{Rot}(\beta) \) is the \( 3 \times 3 \) orthonormal matrix associated to a rotation by an angle \( \beta \) around the \( Z = Z_w \)-axis:

\[ \text{Inertial component} \]

\[ w\ddot{a}_i = \text{Rot}(\theta_w) \left[ \begin{array}{c} a \\ 0 \\ 0 \end{array} \right] + \eta \left[ \begin{array}{c} y \\ -x \\ 0 \end{array} \right]; \]

\[ \text{Centrifugal component} \]

\[ w\ddot{a}_{cr} = \omega^2 \text{Rot}(-\theta_w)[x \quad y \quad 0]^T; \]

\[ \text{Coriolis component} \]

\[ w\ddot{a}_{cr} = 2[0 \quad 0 \quad \omega]^T \times \dot{V}_w \]

where the symbol \( \times \) denotes the vector product.

Fig. 10 displays the inertial, Coriolis and centrifugal components of the apparent acceleration felt by a user in the \( X_w \) and \( Y_w \) directions while walking along a square virtual path with acceleration control commands applied to the platform.
Fig. 11. Sample graphical output of the developed dynamic simulator. The arrows represent (from the right, counterclockwise) the inertial (yellow), centrifugal (red), and Coriolis (green) components of the apparent acceleration felt by the walker on the controlled platform.

Fig. 12. Overview of the components of the CyberCarpet platform (referred to with \{\} in the text).

in Fig. 11, where colored arrows applied to the user body represent the various accelerations felt during a walk on the controlled platform. A video of the square path walk is attached to this paper, while videos of other motion tasks are available at http://www.dis.uniroma1.it/labrob/research/CW.html.

V. DESIGN OF THE SMALL-SCALE PROTOTYPE

This section illustrates the relevant issues in the mechanical design and realization of a small-scale prototype of the CyberCarpet. The general guidelines in the design require the platform to be stiff enough and capable of carrying the weight of a human (100 kg), to react very quickly to the control commands, and to be reliable and easy to interface [29]. Fig. 12 shows an overview of the whole system, including the used test vehicle \{1\}. For further details, the reader is referred to [30].

A. Ball-Array Carpet

The array of balls (see \{2\} in Fig. 12) is one of the most crucial elements of the platform. The resulting motion imposed to the walker strongly depends on a well functioning interaction between belt, balls (with their supporting grid plate), and shoe sole. There are also major haptic issues that influence the perception of the walking surface by the subject. After testing different ball sizes with a number of subjects who provided their impressions, a diameter $d_{bal}$ = 8 mm has been chosen. The ball array is allocated in a supporting grid that keeps the balls in place. The gap between the balls has been set to 0.5 $d_{bal}$ to provide robustness and uniform feeling to the floor.

For determining appropriate materials of belt, balls, and supporting grid, one major aspect concerns the resulting friction forces at the different contact points and surfaces, see Fig. 13. The ideal combination of materials exhibits maximum friction at the belt-ball and ball-shoe contacts, and minimum friction at the ball-grid and grid-belt interfaces. The ball material was chosen as INOX steel, since it is easily available and proven to be a reliable solution. The chosen belt is a Transilion E8/2 U0/V5, from the Fa. Siegling company, which is covered by a soft PVC layer of 0.5 mm displaying a friction coefficient to inox larger than 0.7.

The grid itself can be realized with different materials, comparing their stability and slip-stick parameters. An acetal POM plate manufactured by CNC die-cutting has been selected, leading to friction coefficients of 0.3 and 0.6 with the balls and belt, respectively. The final array contains 4332 balls and fits into an hexagonal grid. The diameters of the inscribed and circumscribed circles are 693 and 800 mm.

B. Belt

The actuated belt \{3\} in Fig. 12 provides the linear velocity command $v$ to the kinematic system (1)–(5). The belt, together with its electrical drive \{4\} and corresponding servo controller \{11\}, is rigidly mounted on the supporting beams \{10\}. In order for the belt to run straight, a proper value for its length-to-width ratio is 1.4. Since the belt width is prescribed by the ball array size, this led to a belt length of 1100 mm. Another issue is the position of the (single) drive actuating the belt, which should always keep the upper strand in a tight span. For this, we placed the drive at the belt center, using an additional pulley placed underneath the belt body: the lower span is thus divided into two small parts and the upper part of the belt is always under direct tension of the actuating force.
C. Turntable

The turntable \( \{9\} \) has to bear the weight of the belt/ball-array system and of the walker on the platform, and provides the angular velocity command \( \omega \) to the kinematic system (1)–(5). The turntable is primarily fixed by the ball bearing \( \{7\} \) in combination with the mounting plate \( \{8\} \), and the actuating torque is applied to the turntable by the drive \( \{14\} \) via the toothed belt \( \{12\} \). Vertical reaction forces are also provided by the support wheels \( \{13\} \) that stabilize the turntable. Since the system should be able to rotate endlessly, current and data lines are fed through the rotational feedthrough \( \{6\} \), which is secured with the ring \( \{5\} \). The whole system is carried by the framework \( \{16\} \) of aluminum beams. The moving (rotating) parts of the whole system supported by this framework weigh about 200 kg.

D. Control and System Drives

The hardware architecture of the control system is shown in Fig. 14. There are two Lenze (9300 series) low-level servocontrollers for the two identical drives of the belt and the turnable. We used two Lenze three-phase motors, type MCA 10, providing a power of 0.8 kW with a supply frequency of 140 Hz. The maximum torque is 2.0 Nm at the speed of 3950 min\(^{-1}\). They actuate the belt through a gear with ratio 1:8.012 and 1:8.217, respectively. As a result, the belt can reach for continuous operation a linear speed of 2 m/s, with a maximum angular velocity and acceleration of the turntable are 2 and 4.4 rad/s\(^2\), respectively.

Both drives are equipped with integrated incremental encoders, and can be controlled up to a maximum sampling frequency of 100 Hz. The servocontroller for the belt drive is mounted on the rotating part of the machine, and uses a RS485 bus for communication. The turntable drive is equipped with a reference switch used to initialize the encoder count for platform orientation. The PC with the high-level control laws sends the velocity inputs \( \nu \) and \( \omega \) via Ethernet to a human machine interface (HMI), where the commands are analyzed and suitably translated to be sent to the low-level servocontrollers. Moreover, the HMI checks the parameters of both drives and controllers to detect unnatural behaviors. This structure provides safety functions to the platform.

VI. VISUAL LOCALIZATION

A visual tracker is used to find the position \((x, y)\), as well as the orientation \( \theta_w \) of the walker, on the CyberCarpet. Our visual tracker is an adaptation of a color-based particle filter [31] and has been tested experimentally at a full scale, with a human user walking (and changing posture) randomly in the field of view of an overlooking camera. The tracker uses a set of particles to model the posterior probability distribution of the state of the walker, i.e., of her/his position on the floor (planar) orientation.

Particle filtering is an estimation approach where multiple hypotheses \( s^{(1)}, \ldots, s^{(N)} \) exist at the same time and are kept during the estimation process. In our application, each hypothesis (or particle) \( s^{(j)} \) represents one possible state of the walker, with a corresponding discrete sampling probability \( \pi^{(j)} \). The particle type considered in [31] consisted of an elliptical blob with a position and a varying size, describing the boundary of the object being tracked. Since the size of the walker is considered to be constant in our case, each particle (the index \( j \) is dropped for compactness) has been initially specified as

\[
\mathbf{s} = \{x, y, \theta_w\}
\]

where \( x \) and \( y \) represent the position of the center of the ellipse and \( \theta_w \) is the orientation angle of the minor axis of the ellipse, which corresponds to the walker forward direction. However, due to perspective changes and the head bobbing about, the appearance of the user changes continuously during the walk, and the localization algorithm was not fully able to track the walker position in a reliable way. Therefore, the model (30) was extended from a simple ellipse to the combination of an elliptical shoulder region and a circular head region, as seen in a top-view of a person and illustrated in Fig. 15. The description of the particle is

\[
\mathbf{s} = \{x, y, \theta_w, c_x, c_y\}
\]

where \( c_x \) and \( c_y \) are the position of the head circle relative to the ellipse center.

The \( N \) particles are initialized using for all of them the same set of values entered manually (by mouse clicks) on the user interface. At each iteration \( t \) of the visual localization algorithm, three steps are performed to compute the updated set of hypotheses from the one available at the previous iteration \( t - 1 \) and the corresponding estimation of the walker position and orientation.
A. Particle Filtering

In the first step, each particle $s_{t-1}$ of the previous iteration is propagated according to a simple dynamic model. In particular, the evolution $s_t$ is computed as

$$s_t = s_{t-1} + w_{t-1}$$

(32)

where $w_{t-1}$ is a multivariate Gaussian random variable that models the walker motion in the time interval between two iterations. This generates the prior distribution of the next state.

B. Color-Based Observation

To test the probability of the evolved particle $s_t$ being a good hypothesis, the current image captured by the overhead camera is observed. A color histogram $p$ is computed for the shoulder region and another histogram $p'$ for the head region. The shoulder region is defined by all the pixels inside the ellipse, excluding those inside the head circle. The head region is defined by all the pixels inside the head circle. The resulting histogram $p$ is normalized and compared to a stored histogram or target shoulder model $q$ (acquired at the tracker initialization) using the Bhattacharyya coefficient $d[p, q]$, which is explained in more detail in [31]. The same is done for $p'$ and target head model $q'$, resulting in $d[p', q']$. The distance between the particle and the target model is defined by the Bhattacharyya distance [32]

$$d = \sqrt{1 - \frac{p p' + \rho(p')^2}{2}}.$$  

(33)

This similarity measure provides a likelihood of each particle that will be used to update the particle set in the next step. In fact, each element $s^{(j)}$ of the particle set can be assigned a probability $\pi^{(j)}$ in terms of the observations (color histogram), namely

$$\pi^{(j)} = \frac{1}{\sqrt{2\pi} \sigma} \exp \left( -\frac{d^2}{2\sigma^2} \right)$$

(34)

where $\sigma$ is the standard deviation of the Gaussian distribution (a constant that can be fine tuned). The $\pi^{(j)}$, $j = 1, \ldots, N$, are further normalized so as to define the discrete posterior probability distribution of the walker state.

C. Updating the Particle Set and Tracker State

The third step of each iteration generates the new set of hypotheses used for updating the tracker state (the new estimation of the walker position and orientation). The new set of $N$ particles is drawn from the current set by choosing the generic particle $s^{(j)}$ with probability $\pi^{(j)}$. Particles are drawn with replacement, so that those with higher probability are in general selected several times. Finally, the updated tracker state is computed as a weighted mean over all the current particles, using their Bhattacharyya distance (33) to the target model as weights.

D. Final Considerations

Given the increased number of degrees of freedom in the adapted model (31), our experiments have shown that a minimum of $N = 5000$ particles are needed to correctly track the walker. This, however, slowed down the visual tracking rate to 3 Hz. Considering the high resolution of the input image and the relative size of the ellipse, it appeared that more pixels than necessary were evaluated for building the histograms. Thus, we introduced a random sampling, picking 500 random points within the ellipse region. These points were stored as a vector of $(x, y)$ positions relative to the ellipse center $(x, y)$ and angle of orientation $\theta$. The same has been done for the head region. The histograms could then be computed faster by evaluating only the pixels corresponding to these points, and the final visual localization algorithm could run up to 17 Hz.

Typical snapshots of the tracker state for a human walker in a room are shown in Fig. 16, where the 3-D particle (30) and the 5-D particle (31) have been used, respectively, in (a) and in (b). It is apparent that the correct posture is lost (at times) in the first case, motivating the use of the extended model. Complete videos of these two human tracking experiments are included in the material accompanying the paper. Note that for the experiments with the small-scale CyberCarpet platform in Section VII, the same visual algorithm working for human walkers was used. Since the walker was replaced by a mobile robot mock-up, the rate of the tracker was limited to 10 Hz without performance loss.

VII. EXPERIMENTAL RESULTS

The velocity-level control algorithms described in Section III have been implemented and validated on the small-scale CyberCarpet prototype described in Section V. The walker was emulated by a differentially-driven tracked mobile robot carrying on top a picture of a human body (see Fig. 17, including at typical camera view with superimposed localization ellipse/circle). Its position on the platform was localized with the technique of Section VI, using a Sony DFW-VL500 Color/VGA camera, with 640 × 480 pixels at 30 fps, placed at about 131 cm over the surface of the carpet.

The testing campaign involved four different motions for the vehicle. In particular, the following scenarios were chosen:

1) standing still off the origin;
2) starting at the origin and moving along a straight line with a constant speed of about 0.22 m/s;
3) starting at the origin and moving along a circular path of radius 0.35 m with a constant speed of about 0.14 m/s;
4) starting at the origin and moving along a circular path of radius 0.35 m with a constant speed of about 0.14 m/s;
4) starting at the origin and moving along a square path of side 0.4 m with a constant linear velocity of about 0.1 m/s, and turning at the corners with an angular velocity of about $\pi/4$ rad/s.

As for the control laws, for the three scenarios $B$ to $D$ where the user is in motion, we comparatively tested the pure static feedback law $v = v_{fb}, \omega = \omega_{fb}$ given in (17), (18) alone against the full feedback/feedforward strategy $v = v_{fb} + v_{ff}, \omega = \omega_{fb} + \omega_{ff}$ of (22)–(24). The parameters of the control laws were set to $k = 4$ in (17), (18), $k_u = 0.3$ in (23), (24), and $\omega_{ff,max} = 0.05$ rad/s as saturation level in (22). Videos of all experiments accompany the paper (also available at http://www.dis.uniroma1.it/labrob/research/CW.html).

A. Standing Still

In the first experiment, the vehicle is placed in the absolute position $(0.2, 0.05)$ m and keeps a zero intentional velocity during the whole experiment. In Fig. 18 the planar absolute trajectory executed under the control law (17), (18) is shown, with a black triangle marker representing the starting position. The corresponding behavior of the linear and angular velocity commands is displayed in Fig. 19. Note that the recovering path in absolute space is close to the straight line predicted in the control analysis of Section III. The discrepancies are due to the presence of noise in the image processing step, to the discrete sampling of the measurements (10 Hz on the position $(x, y)$), and to the discrete sampling of the control output (10 Hz on the commanded platform velocities).

B. Moving at Constant Velocity

In the second experiment, we tested separately the control laws (17), (18) and (22)–(24), i.e., without or with the online velocity estimation and compensation. The robot moves along a straight line with a constant speed of about 0.22 m/s.

1) Pure Feedback Law (17), (18): The absolute trajectory of the vehicle is reported in Fig. 20. The starting point is at $(0, 0.02)$ m (black triangle) and motion proceeds in the negative $y$-direction [−$Y_0$]. As expected, the static feedback (17), (18) is not able to fully compensate the persistent intentional motion, but a steady state is obtained after about 6 s with a non-zero constant position error. The reached equilibrium position is at about $(0.05, 0.23)$ m (this value depends on the chosen control gains) and the control is not able to center the robot. The linear and angular velocity commands are shown in Fig. 21. Note that, after an initial transient, the linear velocity command matches the user intentional velocity, while the angular command is close to zero.

2) Complete Feedback/Feedforward Law (22)–(24): In this case, the additional presence of the feedforward action based on the observer (23), (24) is able to fully recover the platform center despite the persistent intentional motion, similar to what could be obtained by an integral control action. The vehicle starts at $(0.006, 0.022)$ m (black triangle) and moves in the negative $y$-direction as before. After a transient phase, the estimate of the intentional speed converges to the actual value (see Fig. 23) and the control law (22) brings back the robot to the origin (see Fig. 22). The commanded linear and angular platform velocities are shown in Fig. 24. In comparison with Fig. 21, the angular velocity appears now more erratic, especially toward the end of
the motion (i.e., close to the platform center). This effect is due to the presence of the term $1/R$ in the feedforward term $\omega_{ff}$ of (22), which grows unbounded as $R$ goes to zero. The saturation introduced in (22) helps in softening this effect, but cannot avoid some chattering around the origin (see Fig. 25 for the time behavior of $\omega_{ff}$).

C. Moving Along a Circular Path

In this experiment, the vehicle is moving along a circular path of radius 0.35 m with a constant speed of about 0.14 m/s, and, as
1) Pure Feedback Law (17), (18): The absolute trajectory of the vehicle is shown in Fig. 26. As expected, the control law is only able to partially compensate for the intentional motion: the robot is kept within a distance of 0.2 m from the platform, which is anyway smaller than the original dimension of the circular path (0.35 m). The corresponding platform velocity commands are shown in Fig. 27. It is interesting to note that, after the initial transient, the platform linear and angular velocities match the actual linear (0.14 m/s) and angular (0.4 rad/s) velocity of the vehicle, confirming again that a steady-state condition has been reached. At about \( t = 23.5 \) s, the robot stops its motion and is thus brought back to the center of the platform.

2) Complete Feedback/Feedforward Law (22)–(24): Despite the more challenging task for the observer, the complete feedback/feedforward control law is able to keep the user closer to the platform center than in the previous case, as shown by the absolute trajectories in Figs. 26 and 28 for the two experiments. The velocity commands sent to the platform are shown in Fig. 29.

We note that the convergence of the intentional speed estimate is not perfect (see Fig. 30), so that a residual motion around the platform center is still present in Fig. 28. The reason of this behavior is intrinsic to the structure of the proposed observer. Indeed, the estimated velocity is a low-pass filtered version of the actual velocity, with cutoff frequency given by the observer gain \( k_w \). From standard linear analysis, when the input signal (the actual velocity of the vehicle) has a sinusoidal behavior, the observer output will result in a sinusoid with the same frequency, but different amplitude and phase. In particular, since we have set \( k_w = 0.3 \), and the frequency of the input signal is 0.4 rad/s (the angular velocity of the robot), the resulting estimated velocity will be attenuated by \(-4.5\) dB and the phase shift will be 0.92 rad, equivalent to a time delay of about 2.3 s. Therefore, even at steady state, the estimated velocity lags behind the actual one, thus preventing the controller to complete a perfect recovery of the position to the origin. Accordingly, the estimated intentional speed oscillates around its nominal value.

![Fig. 26. Absolute trajectory in the experiment of Section VII-C1 (circular path, with pure feedback control).](image1)

![Fig. 27. Linear and angular velocity commands for the trajectory of Fig. 26.](image2)

![Fig. 28. Absolute trajectory of the car in the experiment of Section VII-C2 (circular path, with feedforward control action).](image3)

![Fig. 29. Linear and angular velocity commands for the trajectory of Fig. 28.](image4)
of 0.14 m/s, before dropping to zero starting from $t = 23.5$ s when the robot suddenly stops.

D. Moving Along a Square Path

In this last experiment, the vehicle travels along a square path of 0.4 m side with constant linear velocity of about 0.1 m/s. The absolute trajectory in the virtual world during the execution of the square path is shown in Fig. 31 (different colors are used for each side). The robot starts from the Init position (black triangle) and moves to the left along Edge 1 of the square. Then it stops, turns 90° counterclockwise, and starts travelling along Edge 2, repeating the same sequence until tracing the complete square. The total motion time is thus approximately 24 s. The mismatch between the actual trajectory in Fig. 31 and the ideal commanded square path is mainly due to slippage of the tracks of the mobile vehicle during motion and, to a less extent, to the inaccurate execution of its commanded velocities.

1) Pure Feedback Law (17), (18): The static feedback law is able to partially compensate for the intentional motion, keeping the vehicle within a circle centered at the origin and having a radius of about 0.2 m (see Fig. 32). The velocity commands sent to the platform are shown in Fig. 33.

2) Complete Feedback/Feedforward Law (22)–(24): The absolute motion for this case is shown in Fig. 34, while the velocity commands sent to the platform are given in Fig. 35. The benefits of the estimation of the intentional velocity are not so evident as
local mobility, due to the presence of a nonholonomic constraint with the presence of a ball-array carpet. Despite of the restricted linear and angular mobility of a treadmill mounted on a turntable that re-centers a user in unlimited locomotion by combining the 4 s of linear motion along each side are not sufficient for convergence with the chosen observer gains. The estimate always lags behind the actual speed: when the vehicle is moving at 0.1 m/s, increasing maximum values of 0.08, 0.094, and 0.098 are reached along the first, second, and third side. Similarly, when the vehicle stops and turns in place at the corners, the estimate drops toward zero though not reaching this final value. Indeed, higher observer gains would largely improve this behavior, but these were not allowed by measurement noise and feasible sampling times.

VIII. CONCLUSION

We have presented the design and implementation of motion control laws for the CyberCarpet, a novel concept of platform that re-centers a user in unlimited locomotion by combining the linear and angular mobility of a treadmill mounted on a turntable with the presence of a ball-array carpet. Despite of the restricted local mobility, due to the presence of a nonholonomic constraint on the instantaneous velocities, the controller is able to keep a freely walking user close to the platform center in a natural way.

The control law is designed at the velocity level as the composition of a feedback and a feedforward action. The nonlinear feedback is a singularity-free version of an input-output linearization law, while the feedforward term is based on an estimation of the unknown walker intentional velocity through a disturbance observer. The feedback gains can be conveniently scaled so as to decrease the control velocities to perception levels that are acceptable by the user. The smoothness of the velocity control law allows a direct extension to the design of an acceleration-level controller, which was performed using the theory of cascaded systems. This enables to take into account also acceleration bounds due to user’s perception constraints, as well as to perform a dynamic analysis of inertial forces acting on the walker.

To validate the CyberCarpet principle and to test the actual performance of the motion control laws, a small-scale platform has been designed and built having in mind scalability properties. In particular, from the mechanical and actuation points of view, the prototype is already capable of sustaining and moving the full weight of a person. Moreover, the method based on particles filter for visual localization by an overhead camera has been already tested on human walkers in arbitrary motion, proving to be quite robust. Using this setup, a series of velocity-level control experiments have been conducted with a mobile robot vehicle as a mock-up of the walking user. Comparison between pure feedback control and the complete feedback/feedforward scheme has shown the benefits of compensating for the unknown intentional velocity, especially for smooth vehicle motion. In particular, the absence of sharp turns allows a faster convergence of the observer to the intentional linear velocity, and thus its full cancellation.

The main limitations that we found were related to the high level of noise in the measurement of the vehicle position, and to the relatively low sampling frequency of the visual localization. The walker’s orientation, though available from visual estimation, has not been used in the control law, thus preventing the prediction of intentional turns and delaying the re-centering. Nonetheless, the robot vehicle never approached dangerously the platform border, proving the effectiveness of velocity-level control up to intentional velocities of 0.25 m/s, comparable to the diameter of 0.8 m of the prototype. At this scale, resort to acceleration control was found not necessary.

Having proven the feasibility of the CyberCarpet concept in all its components, the next step would be the construction of a full-scale device to have a human user walk at normal speed while being immersed in a Virtual Reality environment. Our parallel experience with the other omni-directional belt-array platform developed within the CyberWalk project [16], [17] suggests that the compact mechanical principle underlying the ball-array platform may still be a convenient choice in terms of weight, needed power, ease of maintenance, and reduced part wearing. The total weight of the moving parts of the $5 \times 5 \text{m}$ omni-directional CyberWalk platform is over 7500 kg, with the need of a combined electrical and hydraulic actuation. A full scale ball-array platform with similar performance could be of smaller size/weight and more efficient due to its actuation mech-
anism. In fact, the CyberCarpet tends always to align its main belt with the motion direction of a persistent walking user. Thus, in a steady-state condition, only one dof needs to be actuated, considerably reducing the energy consumption. Conversely, the belt-array CyberWalk platform needs in general full 2-D actuation for compensating a persistent walk. Additional investigations are required to establish the perceptual effects of the combined linear and angular motion imposed by the CyberCarpet on the walker especially during transients, so as to set accordingly control design constraints. The introduced transposition of the smooth control design to the acceleration level represents a needed and useful step.

REFERENCES


Alessandro De Luca (F’07) received the Ph.D. in systems engineering from the University of Roma “La Sapienza”, Rome, Italy, in 1987.

He is a Professor of robotics and automatic control since 2000. His research interests include motion planning and nonlinear control of flexible, redundant, and underactuated manipulators, and of wheeled nonholonomic mobile robots, as well as fault detection and isolation, visual servoing, and physical human-robot interaction. He published about 170 journal and conference papers and book chapters.


Raffaella Mattone received the Laurea degree in electrical engineering and the Ph.D. degree in systems engineering from the University of Roma “La Sapienza”, Rome, Italy, in 1993 and 1997, respectively.

She is currently a teacher of mathematics and physics with a secondary school in Rome. She was Guest Scientist with Fraunhofer IPA, Stuttgart, Germany, (1997–1998) and Research Engineer with Ascom AR&T, Maegenwil, Switzerland (1998–2000). From 2000 to 2008, she was Research Assistant with the Dipartimento di Informatica e Sistemistica (DIS), University of Roma “La Sapienza”. She is author of almost 40 journal and conference papers and book chapters.
papers, and of two European patents, mostly in the field of modeling and control of nonlinear robotic systems.

Paolo Robuffo Giordano (M’08) received the M.Sc. degree in computer engineering and the Ph.D. degree in systems engineering from the University of Roma “La Sapienza”, Rome, Italy, in 2001 and 2008, respectively.

In 2007 and 2008, he spent one year as PostDoc with the Institute of Robotics and Mechatronics, German Aerospace Center. At the end of 2008, he moved to the Max Planck Institute for Biological Cybernetics, Tübingen, Germany, where he is currently Senior Research Scientist and head of the Human-Robot Interaction Group. His research interests span nonlinear control, robotics, haptics, and VR applications.

Heinz Ulbrich received the Ph.D. degree from Technical University of Munich (TUM), Munich, Germany, in 1979.

He is Full Professor of applied mechanics with the TUM, Munich, Germany. He was a Senior Research Fellow with NASA Lewis Research Center, Cleveland, OH, and then a Professor with the Technical University of Braunschweig and the University of Essen. He has been a member of the Advisory Panel of NATO’s Physical and Engineering Sub-Programme, of the EUROMECH Solid Mechanics Conference Committee, of the Council Board of GAMM, and of the Foundation Boards of the Likar Stiftung and Timoshenko Stiftung. With more than 300 scientific publications, including 60 papers in peer-reviewed journals and three books, his main research activities cover multi-body systems with one-sided and two-sided constraints, nonlinear vibrations, mechanical systems with variable time structure, regulation and optimization of vibration systems, with applications to drive trains in machines and vehicles, gearbox vibrations, elastic robots and mechanisms, humanoid robots, and walking machines.

Martin Schwaiger received the Diplomingenieur degree in industrial engineering from the University of Applied Sciences, Munich, Germany, in 2002, with a thesis on an autonomous wall-climbing robot, and the M.Sc. degree in management from the Grenoble Ecole de Management, Grenoble, France, in 2003, and the Ph.D. degree from the Technical University Munich (TUM), Munich, Germany, in 2008.

In 2003, he started his industrial career at the logistic company Jungheinrich AG, dealing with new technologies for warehouse control. He joined the CyberWalk Team, Institute of Applied Mechanics, TUM, at the beginning of the project, being responsible for the mechanical and electrical design of the two developed platforms. Since then he has been with Jungheinrich, where he is currently in charge of a novel auto pallet mover system.

Michael Van den Bergh (M’05) received the M.Sc. degree in electrical engineering from the Katholieke Universiteit Leuven, Leuven, Belgium, in 2004, with a thesis on the VISICS Lab of the Electrical Engineering Institute (ESAT), and the Ph.D. degree from ETH Zurich, Zurich, Switzerland, in 2010, with a thesis on “Visual Body Pose Analysis for Human-Computer Interaction”.

In 2005, he joined the Computer Vision Lab, ETH Zurich, working as a Research Assistant in the field of Human-Computer Interaction.

Esther Koller-Meier received the M.Sc. degree in computer science and the Ph.D. degree from ETH Zurich, Zurich, Switzerland, in 1995 and 2000, respectively.

Until 2009, she worked as a PostDoc within the Computer Vision Lab, ETH Zurich. Her research interests include object tracking, gesture analysis, and multi-camera systems. She is currently with the Swiss Academy of Engineering Sciences, Zurich, Switzerland.

Luc Van Gool received the Ph.D. degree in electro-mechanical engineering, Katholieke Universiteit, Leuven, Belgium, in 1981.

Currently, he is a Professor with the Katholieke Universiteit Leuven and the ETH Zurich, Zurich, Switzerland. At both sites, he leads computer vision research and teaches computer vision. He has authored over 200 papers in this field. His main interests include 3-D reconstruction and modeling, object recognition, and action and gesture analysis. He is a co-founder of the companies Eyetronics, koorba, GeoAutomation, Procedural, and eSaturnus.

Dr. Gool was a recipient of several Best Conference Paper Awards (e.g., at ICCV98, CVPR07, ACCV07, ICRA09, BMVC11). He was Program Chair of ICCV 2005 and General Chair of ICCV 2011. In 2011, he was awarded an ERC Advanced Grant.